

# Performance of Golden encoded MIMO OFDM system with carrier frequency offset

Dr.C.Geetha Priya

## ABSTRACT

This paper presents the performance of carrier Frequency offset estimation algorithm for golden encoded MIMO OFDM system. Basically Algebraic Space Time Code (ASTC) has three major encoding methods they are Golden, TAST and DAST encoding. But Golden encoder provides an efficient performance while compared with the TAST and DAST. Carrier frequency offset estimated for Golden code multiple input and multiple output (MIMO) Orthogonal frequency division multiplexing (OFDM) system. The orthogonal training sequence are simultaneously transmitted and received from multiple antennas. In the receiver side estimated the Carrier frequency offset (CFO), Golden code gives the efficient SNR vs. MSE compared with the Cramer Rao Lower Bound (CRLB).

**Keyword**-Algebraic Space Time Code (ASTC), Multi Input and Multi Output (MIMO), Orthogonal frequency division multiplexing (OFDM), Carrier frequency offset (CFO), Cramer Rao Lower Bound (CRLB).

## 1. Introduction

To improve the data rate and error free data transmission Algebraic Space Time Code are used. A golden encoding method is used to achieve a full rate and full diversity for transmission. Carrier frequency offset is estimated in the receiver side. SNR vs. MSE is compared with Golden encoded MIMO OFDM system and the theoretical CRLB.

The space time codes have good performance, but they suffer from the non-uniform distribution of the energy in the code word. To alleviate this problem, a new family of ASTCs has been proposed in [1] and [2], which have a structure of full-rate and full-diversity  $2 \times 2$ ,  $3 \times 3$ ,  $4 \times 4$ , and  $6 \times 6$  space-time codes. These codes have a constant minimum determinant as spectral efficiency increases. The name perfect space-time codes, which is used for these codes, is suggested by the fact that they satisfy a large number of design criteria and only appear in a few special cases of the classical perfect error-correcting codes, achieving the Hamming sphere-packing bound. In this paper,  $2 \times 2$  and  $4 \times 4$  perfect codes are used.

Orthogonal frequency-division multiplexing (OFDM) has been adopted in the wireless local area network standards IEEE 802.11a [3] and g [4] due to its high spectral efficiency and ability to deal with frequency-selective fading. The combination of OFDM with spectrally efficient multiple-antenna techniques makes the OFDM a good candidate to overcome the frequency selective problems for the perfect  $2 \times 2$  and  $4 \times 4$  ASTC codes.

Despite the attractive features of both OFDM and ASTC, they are very sensitive to transmitter-receiver synchronization imperfections [5]. Thus, the synchronization is crucial for ASTC-multiple-input-multiple-output (MIMO)-OFDM-based systems. Frequency synchronization errors destroy the orthogonality among the subcarriers, which results in inter carrier interference (ICI) [6]. Therefore, an accurate carrier frequency offset (CFO) estimation is essential for OFDM receiver design. Various carrier synchronization schemes have been proposed for single-input-single-output OFDM systems. Some schemes rely on pilot or preamble data [8]-[14], and some use the inherent structure of the OFDM symbol in either frequency [15] or time domain [16]. For multiple-antenna OFDM, data-aided schemes are proposed for receiver diversity and MIMO in [17] and [18], respectively. A blind method for receiver diversity combined with OFDM is proposed in [19].

## 2. System model

The system model consists of Algebraic Space Time Code encoder and decoder; Orthogonal Frequency Division Multiplexing modulator and demodulator; Multiple Input Multiple Output transmitting and receiving antennas. These models are explained in following sections.

### A. MIMO OFDM MODEL

A multicarrier system can be efficiently implemented in discrete time using an inverse DFT (IDFT) to act as a modulator and a DFT to act as a demodulator. The transmitted data are the "frequency" domain coefficients and the samples at the output of the IDFT stage are "time" domain samples of the transmitted waveform. Fig.1 shows a typical ASTC MIMO-OFDM system for Golden Encoder.

Consider the baseband-equivalent ASTC-MIMO OFDM system, with  $nt$  transmit antennas and  $nr$  receive antennas, depicted in Fig. 1. The transmitted binary source sequence  $sk$  is quadrature phase-shift keying (QPSK) modulated. The QPSK symbols are then ASTC encoded.

### B. GOLDEN ENCODER

Each information in the sequence of data at time  $n_i$  is encoded by the ASTC encoder into two stream constellations represented by the code word  $X_{n_i} \times N_i$ , where  $N_i$  refers to number of transmitted antennas and  $N_c$  is the number of used subcarriers

The code is a  $1 \times 128$  STBC obtained using a division algebra, which is full rate, full diversity, and has a nonzero lower bound on its coding gain, which does not depend on the constellation size.

Code word in the form of  $2 \times 2$  is written as:

$$X_{n_i} = \frac{1}{\sqrt{5}} \begin{pmatrix} \alpha(v_{n_i}(1) + \theta v_{n_i}(2)) & \alpha(v_{n_i}(3) + \theta v_{n_i}(4)) \\ \bar{\alpha}(v_{n_i}(3) + \bar{\theta} v_{n_i}(4)) & \bar{\alpha}(v_{n_i}(1) + \bar{\theta} v_{n_i}(2)) \end{pmatrix} \quad (1)$$

Where,

$$\theta = \frac{1 + \sqrt{5}}{2}, \quad \bar{\theta} = \frac{1 - \sqrt{5}}{2}$$

$$\alpha = 1 + i - i\theta; \quad \bar{\alpha} = 1 + i - i\bar{\theta}$$

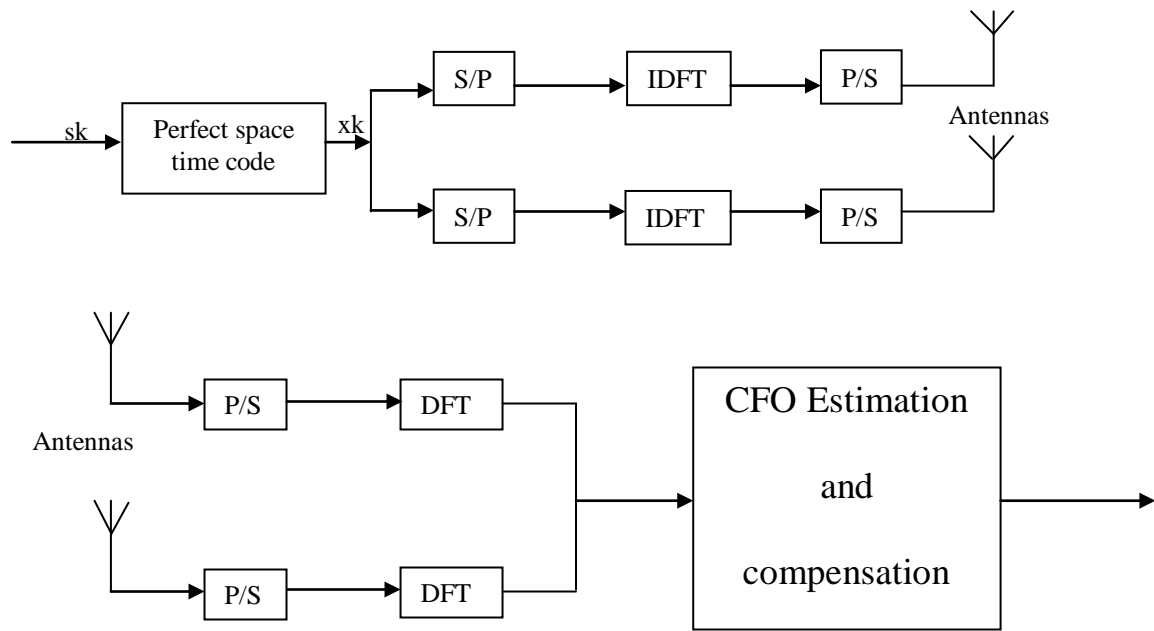


Fig 1. ASTC MIMO OFDM system for Golden Encoder

### 3. Carrier Frequency Offset Estimation Algorithm

In Carrier Frequency Offset estimation algorithm the first step is receiving the transmitted signal. The received signal has Carrier frequency offset and noise with it. The received signal  $r_x$  can be represented as given below.

$$r_x = (u_x \cdot H_x) + w \quad (2)$$

In this equation  $w$  is additive noise and  $H_x$  is the channel with the received signal. From this the Carrier Frequency Offset should be estimated. The following equations explain how the CFO is estimated from the received signal.

$$\hat{c} = r_x (e^{j\pi\Delta}) \quad (3)$$

$$\hat{\Delta} = \angle \left( \sum_0^{N-1} \frac{\hat{c}}{r_x} \right) \quad (4)$$

In the equation  $\hat{c}$  the symbol has values less than 1. The Carrier Frequency Offset can be estimated from the equation and it is the estimated CFO. This estimation can be done with Golden encoders.

$$CRLB = \frac{n_c \sigma^2}{16\pi^{4n_r}} \quad (5)$$

### 4. Simulation Results and Discussion

Consider an OFDM symbol with a total of  $N = 128$  subcarriers and no virtual subcarriers. Here two antennas are used at

both transmitter and receiver side. So, number of transmitter  $n_t$  is 2 and number of receiver  $n_r$  is 2. The data generated are in the form of a row vector and size of the vector is  $1 \times 128$ . The simulation results are as follows.

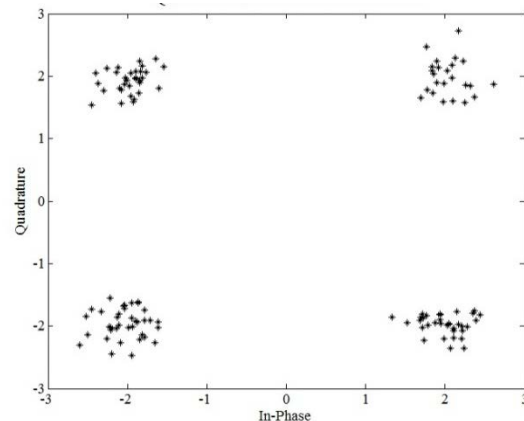


Fig 2. QPSK Constellation for  $1 \times 128$  data

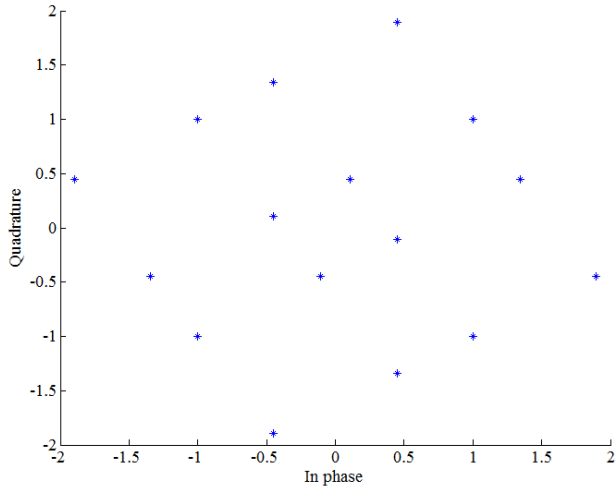


Fig 3. Constellation for Golden Encoder

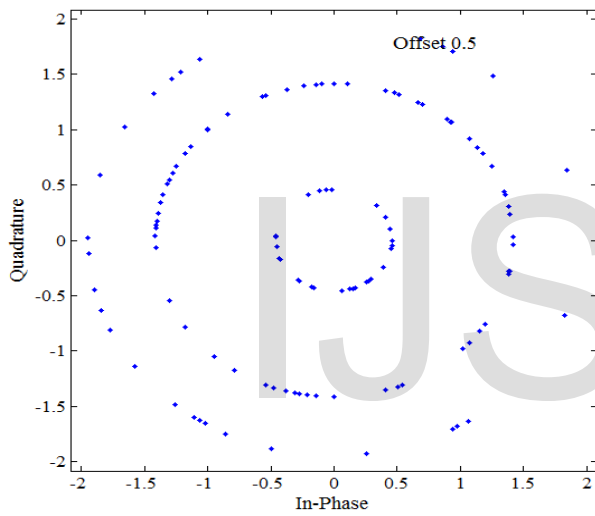


Fig 4. Golden Encoder with offset 0.5 subcarrier spacing

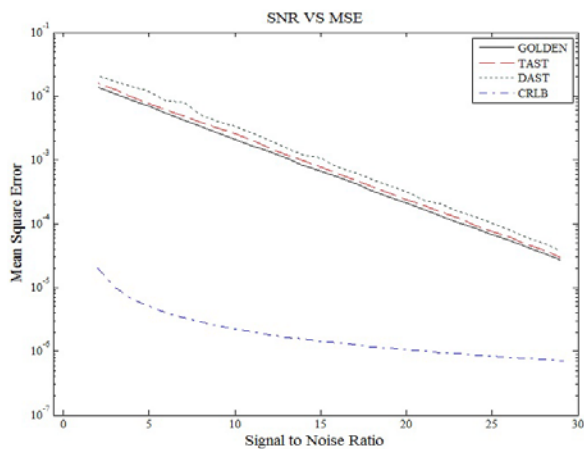


Fig 5. SNR Vs. MSE for ASTC Encoded MIMO OFDM

SNR	MSE		
	GOLDEN	TAST	DAST
0	0.02226	0.02446	0.03513
1	0.01690	0.01979	0.02588
2	0.01372	0.01596	0.02082
3	0.01076	0.01251	0.01676
4	0.00868	0.00971	0.01409
5	0.00690	0.00772	0.01185
6	0.00534	0.00602	0.00830
7	0.00426	0.00485	0.00803
8	0.00337	0.00393	0.00509
9	0.00263	0.00311	0.00405
10	0.00211	0.00253	0.00335
11	0.00163	0.00201	0.00264
12	0.00135	0.00152	0.00206
13	0.00106	0.00119	0.00151
14	8.2994E-4	9.6445E-4	0.00118
15	6.7159E-4	7.7450E-4	0.00107
16	5.3794E-4	6.0307E-4	7.7302E-4
17	4.2306E-4	4.8399E-4	6.3186E-4
18	3.2465E-4	3.8329E-4	5.0056E-4
19	2.6077E-4	3.0142E-4	3.8689E-4
20	2.0926E-4	2.3960E-4	3.1584E-4
21	1.6756E-4	1.9622E-4	2.3182E-4
22	1.3129E-4	1.5196E-4	2.0679E-4
23	1.0557E-4	1.2328E-4	1.5918E-4
24	8.4538E-5	9.3325E-5	1.2767E-4
25	6.7037E-5	7.4907E-5	1.0166E-4
26	5.4192E-5	6.2010E-5	8.1223E-5
27	4.2728E-5	4.7470E-5	6.0949E-5
28	3.4391E-5	3.7969E-5	4.8535E-5

Table 1. Performance Comparison of CFO estimation algorithm for Golden, TAST and DAST encoded MIMO OFDM system.

This results shows that the comparison with the Golden code SNR Vs. MSE ratio to the CRLB SNR Vs. MSE ratio. The result shows that the Golden Encoder is closely to Cramer-Rao lower bound plot.

## 5. Conclusion

This paper presented a new algebraic CFO estimation technique for MIMO-OFDM systems over AWGN channel employing ASTC Golden Encoder. The results of CFO estimation are perfect and by using Golden encoders full rate and full diversity are achieved. The simulated results shows that the Golden Encoder approaches to the theoretical Cramer-Rao lower bound .

## 6. Reference

- [1] J. C. Belfiore, G. Rekaya, and E. Viterbo, "The golden code: A  $2 \times 2$  full-rate space-time code with nonvanishing determinants," *IEEE Trans. Inf. Theory*, vol. 51, no. 4, pp. 1432–1436, Apr. 2005.
- [2] S. Yang, J. C. Belfiore, G. Rekaya, and B. Othman, "Perfect spacetimeblock codes for parallel MIMO channels," *IEEE Trans. Inf. Theory*, vol. 13, pp. 1949–1953, Jul. 2006.
- [3] Information Technology- Telecommunications and Information Exchange Between Systems- Local and Metropolitan Area Networks-Specific Requirements  
Part 11: Wireless LAN Medium Access Control (MAC) and Physical Layer (PHY) Specifications Amendment 1: High-Speed Physical Layer In the 5 GHz Band, ISO/IEC 8802-11:1999/Amd 1:2000(E); IEEE Std. 802.11a, 2000.
- [4] Further Higher-Speed Physical Layer Extension in the 2.4 GHz Band, IEEE Std. 802.11g, 2003.
- [5] A. Bannour, M. L. Ammari, Y. Sun, and R. Bouallegue, "On the capacity of ASTC-MIMO-OFDM system in a correlated Rayleigh frequency selective channel," in *Proc. IEEE 73rd VTC Spring*, 2011, pp. 1–5.
- [6] A. H. Al-Dweik and M. R. Renfors, "Blind estimation of large carrier frequency offset in wireless OFDM systems," *IEEE Trans. Veh. Technol.*, vol. 56, no. 2, pp. 965–968, Mar. 2007. BANNOUR et al.: CFO ESTIMATOR FOR ASTC-MIMO-OFDM SYSTEMS 2475
- [7] A. Salberg and A. B. Swami, "Doppler and frequency-offset synchronization in wideband OFDM," *IEEE Trans. Wireless Commun.*, vol. 4, no. 6, pp. 2870–2881, Nov. 2005.
- [8] P. H. Moose, "A technique for orthogonal frequency division multiplexing frequency offset correction," *IEEE Trans. Commun.*, vol. 42, no. 10, pp. 2908–2914, Oct. 1994.
- [9] M. Morelli and U. Mengali, "An improved frequency offset estimator for OFDM applications," *IEEE Commun. Lett.*, vol. 3, no. 3, pp. 75–77, Mar. 1999.
- [10] H.-K. Song, Y.-H. You, J.-H. Paik, and Y.-S. Cho, "Frequency-offset synchronization and channel estimation for OFDM-based transmission," *IEEE Commun. Lett.*, vol. 4, no. 3, pp. 95–97, Mar. 2000.
- [11] Y. Sun, Z. Xiong, and X. Wang, "EM-based iterative receiver design with carrier-frequency offset estimation for MIMO-OFDM systems," *IEEE Trans. Commun.*, vol. 53, no. 4, pp. 581–586, Apr. 2005.
- [12] T. Roman, M. Enescu, and V. Koivunen, "Joint time-domain tracking of channel and frequency offsets for MIMO-OFDM systems," *Wireless Pers. Commun.*, vol. 31, no. 3/4, pp. 181–200, Dec. 2004.

- [13] H. Minn, N. Al-Dhahir, and Y. Li, "Optimal training signals for MIMO OFDM channel estimation in the presence of frequency offset and phase noise systems," *IEEE Trans. Commun.*, vol. 54, no. 10, pp. 1754–1759, Oct. 2006.
- [14] M. Ghogho and A. Swami, "Training design for multipath channel and frequency-offset estimation in MIMO systems," *IEEE Trans. Commun.*, vol. 54, no. 10, pp. 3957–3965, Oct. 2006.
- [15] U. Tureli, L. Hui, and M. Zoltowski, "A high efficiency carrier estimator for OFDM communications," in *Proc. 31st Asilomar Conf. Signals, Syst. Comput.*, 1997, pp. 505–509.
- [16] J. J. van de Beek, M. Sandell, and P. O. Borjesson, "ML estimation of time and frequency offset in OFDM systems," *IEEE Trans. Signal Process.*, vol. 45, no. 7, pp. 1800–1805, Jul. 1995.
- [17] A. Czylik, "Synchronization for systems with antenna diversity," in *Proc. IEEE VTS 50th VTC-Fall*, 1999, vol. 2, pp. 728–732.
- [18] A. N. Mody and G. L. Stüber, "Synchronization for MIMO OFDM systems," in *Proc. IEEE Global Telecommun. Conf.*, 2001, pp. 509–513.
- [19] U. Tureli, D. Kivanc, and H. Liu, "Multicarrier synchronization with diversity," in *Proc. IEEE VTS 54th Veh. Technol. Conf. VTC-Fall*, 2001, pp. 952–956.
- [20] Y. Xiao, X. Lei, and S. Li, "Improved CP-based carrier frequency offset estimator for OFDM systems," in *Proc. Int. Conf. Wireless Commun., Netw. Mobile Comput.*, 2007, pp. 209–211.